# **Useful Constants**

		Common Powers of 19		
speed of light $c = 2.998 \times 10^{\circ} m/s$ basic upit of charge $c = 1.602 \times 10^{-19} C$	Value	Name	Prefix	
gravitational constant $G = 6.674 \times 10^{-11} N m^2/ka^2$	$10^{-12}$	pico	р	
mass of electron: $m_c = 9.109 \times 10^{-31} kg$	$10^{-9}$	nano	n	
$\epsilon_o = 8.854 \times 10^{-12} \ C^2 / (N \ m^2)$	$10^{-6}$	micro	$\mu$	
$\epsilon_{o} = 8.854 \ pF/m$	$10^{-3}$	milli	m	
$k = \frac{1}{4} = 8.988 \times 10^9 \ N \ m^2/C^2$	$10^{-2}$	centi	с	
acc to due gravity (standard) $a = 9.807 \ m/s^2$	$10^{-1}$	deci	d	
Sun: $mass = 1.99 \times 10^{30} ka$ , $radius = 6.96 \times 10^8 m$	$10^{3}$	kilo	k	
Earth: $mass = 5.97 \times 10^{24} ka$ , $radius = 6.38 \times 10^6 m$	106	mega	Μ	
Charge densities: $\lambda = Q/length$ , $\sigma = Q/area$ , $\rho = Q/volume$	$10^9$	giga	G	

**Random Physics 1 equations:**  $\Sigma \vec{F} = m\vec{a}$ If constant acc:  $x(t) = x_o + v_{ox}t + \frac{1}{2}a_xt^2 \quad || \quad v_x(t) = v_{ox} + a_xt \quad || \quad v_x^2 = v_{ox}^2 + 2a_x\Delta x$ Work and Energy:  $W_{a\ to\ b} = \int_a^b \vec{F} \cdot d\vec{l} \quad || \quad K_b = K_a + \Sigma W \text{ or } (K_b + U_b) = (K_a + U_a) + \Sigma W_{other}$   $K = \frac{1}{2}mv^2 \quad || \quad \text{Uniform circular motion:} \quad a_c = v^2/r \quad || \quad \text{Period:} \quad T = 2\pi r/v$ 

**Coulomb's Law:**  $F = k|q_1q_2|/r^2$ . Matching signs repel; different signs attract.

Flux:  $\Phi_E = \int \vec{E} \cdot d\vec{A}$ . Gauss's Law:  $\Phi_E = Q_{encl}/\epsilon_o$  when flux integrated over a closed surface.

Electric field:  $\vec{E} = \vec{F}/q_o$ .  $\vec{E}$  points out from positive charges, in towards negative charges.

Charge Distribution	Point of interest	Electric field
point charge Q	distance r from Q	$E = kQ/r^2$
conducting sphere	outside $(r > R)$	$E = kQ/r^2$
	inside $(r < R)$	E = 0
nonconducting sphere	outside	$E = kQ/r^2$
infinite wire	distance r from wire	$E = \lambda / (2\pi\epsilon_o r)$
conducting cylinder	outside	$E = \lambda / (2\pi\epsilon_o r)$
	inside	E = 0
infinite sheet	any point	$E = \sigma / (2\epsilon_o)$
pair of sheets of opposite charge	between plates	$E = \sigma / \epsilon_o$
line segment $a = L/2$	along axis $\perp$ to midpoint	$E = kQ/(x\sqrt{x^2 + a^2})$
line segment $a = L/2$	along axis $\perp$ to midpoint	$E = 2k\lambda/(x\sqrt{(x/a)^2 + 1})$
ring of radius $a$	along axis $\perp$ to ring center	$E = kQx/(x^2 + a^2)^{3/2}$
charged disk radius R	along axis $\perp$ to disk center	$E = \frac{\sigma}{2\epsilon_o} \left(1 - \frac{1}{\sqrt{(R^2/x^2) + 1}}\right)$

# Geometry:

circle:  $C = 2\pi r, A = \pi r^2$ sphere:  $C = 2\pi r$ ,  $A = 4\pi r^2$ ,  $V = \frac{4}{3}\pi r^3$ cylinder:  $A = 2\pi rh$ ,  $V = \pi r^2h$ 

Common Integrals:  $\int x^n dx = \frac{x^{n+1}}{n+1} \text{ for } n \neq -1$  $\int_{1}^{\infty} \frac{1}{x} dx = ln(x)$  $\int_{1}^{\infty} e^{ax} dx = \frac{1}{a} e^{ax}$ (If you need others I will look them up.)

### Potential energy and Potential

$$\begin{split} V &= U/q_o \text{ or } U = q_o V \\ 2 \text{ point charges (or equiv): } U &= kqq_o/r \qquad V = kq/r \\ \text{n point charges (or equiv): } U &= kq_o \sum \frac{q_i}{r_i} \qquad V = k \sum \frac{q_i}{r_i} \\ \text{distribution: } U &= kq_o \int \frac{dq}{r} \qquad V = k \int \frac{dq}{r} \\ \text{infinite line of charge: } V &= \frac{\lambda}{2\pi\epsilon_o} ln(\frac{r_o}{r}) \\ \text{cylinder of charge (radius R): } V &= \frac{\lambda}{2\pi\epsilon_o} ln(\frac{R}{r}) \text{ (for } r > R) \\ \text{ring of radius } a \text{, along line } \bot \text{ to plane of ring: } V &= kq/\sqrt{x^2 + a^2} \end{split}$$

## Capacitance

C = Q/Vparallel plates:  $C_o = \epsilon_o A/d$ spherical capacitor:  $C_o = 4\pi\epsilon_o \frac{r_a r_b}{r_b - r_a}$ cylindrical capacitor:  $C_o = 2\pi\epsilon_o L/\ln(r_b/r_a)$ series:  $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \cdots$ parallel:  $C = C_1 + C_2 + \cdots$ energy stored:  $U = \frac{Q^2}{2C} = \frac{1}{2}CV^2 = \frac{1}{2}QV$ energy density:  $u = \frac{1}{2}\epsilon_o E^2$ dielectrics:  $C = C_o K$   $E = E_o/K$ 

Kirchhoff: Junction (node) rule:  $\Sigma I_{in} = \Sigma I_{out}$ 

e) rule:  $\Sigma I_{in} = \Sigma I_{out}$  Loop rule

RC circuits:  $\tau = RC$ charging:  $Q = C\xi(1 - e^{-t/\tau})$   $I = dQ/dt = \frac{\xi}{R}e^{-t/\tau}$   $V_C = Q/C = \xi(1 - e^{-t/\tau})$ discharging:  $Q = Q_o e^{-t/\tau}$   $I = dQ/dt = I_o e^{-t/\tau}$   $V_C = Q/C = V_o e^{-t/\tau}$ 

<b>Dielectric Constants</b> (at $20^{\circ}C$ )				
	Dielectric	Dielectric		
	$\operatorname{constant}$	strength		
Material	K	(V/m)		
Vacuum	1.0000			
Air (1 atm)	1.0006	$3 \times 10^6$		
Paraffin	2.2	$10 \times 10^6$		
Polystyrene	2.6	$24 \times 10^6$		
Vinyl (plastic)	2  to  4	$50 \times 10^6$		
Paper	3.7	$15 \times 10^6$		
Quartz	4.3	$8 \times 10^6$		
Oil	4	$12 \times 10^6$		
Glass, pyrex	5	$14 \times 10^6$		
Porcelain	6 to 8	$5 \times 10^6$		
Mica	7	$150 \times 10^6$		
Water (liquid)	80	$150 \times 10^6$		

<b>Resistivity and Temperature Coefficients</b>				
$\rho = \rho_o [1 + \alpha (T - T_o)]$ where $T_o = 20^{\circ} C$				
Material	$\rho_o \ (\Omega \cdot m)$	$\alpha (^{o}C)^{-1}$		
Conductors				
Silver	$1.59 \times 10^{-8}$	0.0061		
Copper	$1.68 \times 10^{-8}$	0.0068		
Gold	$2.44\times10^{-8}$	0.0034		
Aluminum	$2.65 \times 10^{-8}$	0.00429		
Tungsten	$5.60 \times 10^{-8}$	0.0045		
Iron	$9.71 \times 10^{-8}$	0.00651		
Platinum	$10.60 \times 10^{-8}$	0.003927		
Mercury	$98.00 \times 10^{-8}$	0.0009		
Nichrome	$100.00 \times 10^{-8}$	0.0004		
Insulators				
Glass	$10^9$ to $10^{12}$			
Hard rubber	$10^{13}$ to $10^{15}$			

Current, Resistance...  $I = dQ/dt = n|q|v_dA$ temperature variation:  $\rho = \rho_o[1 + \alpha(T - T_o)]$ Ohm's law:  $V_{ba} = IR$  where  $R = \rho L/A$ parallel:  $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \cdots$ series:  $R = R_1 + R_2 + \cdots$ EMF  $\xi$ : ideal output of source
battery internal resistance:  $V_{ba} = \xi - Ir$ Power:  $P = V_{ba}I = I^2R = V_{ba}^2/R$ AC:  $V = V_o \sin(\omega t)$   $I = I_o \sin(\omega t)$   $P_{avg} = I_{rms}V_{rms} = I_{rms}^2R = V_{rms}^2/R$   $I_{rms} = \frac{1}{\sqrt{2}}I_o$   $V_{rms} = \frac{1}{\sqrt{2}}V_o$ 

Loop rule:  $\Sigma \Delta V = 0$