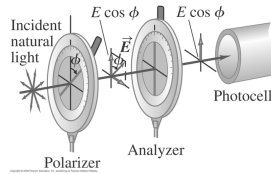
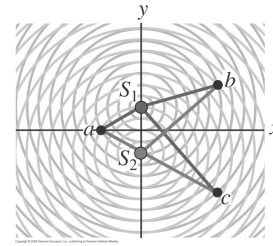


Polarization by reflection
 $\tan \theta_p = n_b/n_a$



Outgoing light polarized at filter angle
 If polarized in: $I = I_o \cos^2 \phi$
 If unpolarized in: $I = \frac{1}{2} I_o$

2-source interference (general)



Path difference: Δs
 Constructive: $\Delta s = m\lambda$
 Destructive: $\Delta s = (m + \frac{1}{2})\lambda$

2-source interference (far-field)

(far-field: $R > 10d$)

Constructive Interference:

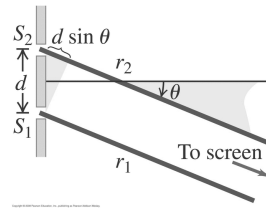
$$d \sin \theta = m\lambda \text{ for } m = 0, \pm 1, \pm 2, \dots$$

Destructive Interference:

$$d \sin \theta = (m + \frac{1}{2})\lambda \text{ for } m = 0, \pm 1, \pm 2, \dots$$

Bright fringes (small θ : $d > 10\lambda$):

$$y_m = m \frac{R\lambda}{d} \text{ for } m = 0, \pm 1, \pm 2, \dots$$



Thin film interference if **NO** relative phase shift

Constructive Interference: $2t = m\lambda_{film}$ for $m = \pm 1, \pm 2, \dots$

Destructive Interference: $2t = (m + \frac{1}{2})\lambda_{film}$ for $m = 0, \pm 1, \pm 2, \dots$

Thin film interference **WITH** half-cycle phase shift

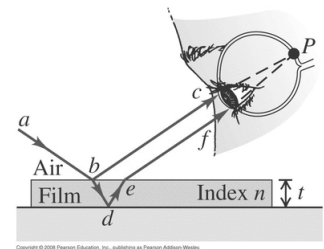
Constructive Interference: $2t = (m + \frac{1}{2})\lambda_{film}$ for $m = 0, \pm 1, \pm 2, \dots$

Destructive Interference: $2t = m\lambda_{film}$ for $m = \pm 1, \pm 2, \dots$

HALF-CYCLE phase shift will occur for reflections

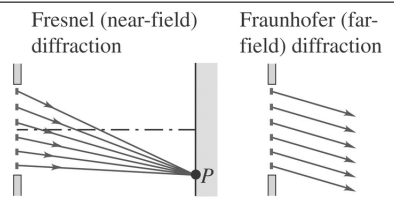
at interface where n increases.

WARN: λ_{film} is wavelength IN MEDIUM, so $\lambda_{film} = \lambda_o/n_{film}$



Diffraction : waves pass through aperture or around an edge.

- Fresnel: nearby source or observer.
- Fraunhofer (typical case): source and observer far away (relative to size of slit)



Single Slit Diffraction (far-field: $R > 10D$)

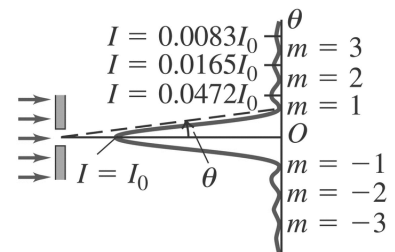
monochromatic waves (light, etc), slit width D

DARK fringes at: $\sin \theta = m \frac{\lambda}{D}$ for $m = \pm 1, \pm 2, \dots$

Small angles: $y_m = m \frac{R\lambda}{D}$ for $m = \pm 1, \pm 2, \dots$

$I(\theta) = I_o \text{sinc}^2(\beta/2)$ where $\text{sinc}(x) \equiv \frac{\sin x}{x}$ and $\beta = \frac{2\pi D \sin \theta}{\lambda}$

Intensity at BRIGHT fringes: $I_m \approx \frac{I_o}{(m + \frac{1}{2})^2 \pi^2}$ for $m = 1, 2, 3, \dots$



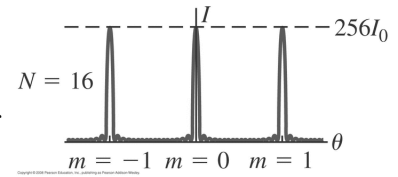
Diffraction Grating (far-field)

large number of parallel slits separated by d

Sharp BRIGHT fringes at: $d \sin \theta = m\lambda$ for $m = 0, \pm 1, \pm 2, \dots$

Small angles: $y_m = m \frac{R\lambda}{d}$ for $m = 0, \pm 1, \pm 2, \dots$

Same effect with REFLECTION grating formed from tiny thin strips of reflecting material (d now being distance between centers of reflecting strips)



Rayleigh resolution limit

single slit of width D : $\sin \theta = \lambda/D$

(Note: $\sin \theta \approx \theta$ if θ is small and in radians)

circular aperture of diameter D : $\sin \theta = 1.22\lambda/D$

Miscellaneous

Speed of sound in air: $v \approx 343 \text{ m/s}$

Speed of sound in water: $v \approx 1500 \text{ m/s}$

Speed of light in vacuum: $v = c = 2.998 \times 10^8 \text{ m/s}$ ($c = 3 \times 10^8 \text{ m/s}$ is good enough)

Light year: $1 \text{ LY} = 9.461 \times 10^{15} \text{ m}$

Energy: $1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$ $K = \frac{1}{2}mv^2$

Typical indices of refraction: $n_{\text{air}} = 1.00$, $n_{\text{water}} = 1.33$, $n_{\text{glass}} = 1.5 \text{ to } 1.8$

Visible light: 390 nm to 750 nm (see table below)

Audible range (humans): $f = 20 \text{ Hz}$ to $f = 20,000 \text{ Hz}$

Nanometer: $1 \text{ nm} = 10^{-9} \text{ m}$ Frequency, wavelength and wave speed: $v = \lambda/T = \lambda f$.

Arc-length: $s = r\theta$ (angle in radians)

Quadratic equation: if $ax^2 + bx + c = 0$ then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Far Field : $R > 10d$ or $R > 10D$ with R being the distance away from the slit/aperture/grating

Small Angle : $d > 10\lambda$ or $D > 10\lambda$

(We didn't develop near-field equations for single slit or diffraction gratings, so it's OK to use the far-field equations for those.)

Light	
Wavelength λ (nm)	Color
< 390	(ultraviolet)
390 – 435	Violet
435 – 500	Blue
500 – 520	Cyan
520 – 565	Green
565 – 590	Yellow
590 – 625	Orange
625 – 750	Red
> 750	(infrared)

FM radio: λ around 2.78 m to 3.41 m

AM radio: λ around 176 m to 555 m

Digital TV: λ around 40 cm